Measurements of Turbulent Fluxes of Momentum and Sensible Heat over the Labrador Sea

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ABSTRACT

Turbulent fluxes of momentum and sensible heat were estimated from sonic anemometer measurements gathered over the Labrador Sea during a winter cruise of the R/V Knorr. The inertial dissipation method was used to calculate turbulent fluxes of momentum. The resulting drag coefficients agree well with earlier findings. Sensible heat fluxes were computed using both cross-correlation and inertial dissipation techniques. There is good agreement between results from both methods, although there is more scatter in the correlation fluxes than the dissipation fluxes. The inertial dissipation method gives reasonable results even under conditions of high wind speeds and low air temperatures, which combined with the relatively warm sea surface temperatures lead to sensible heat fluxes of several hundred watts per square meter. Sensible heat fluxes obtained from the sonic anemometer measurements agree well with bulk turbulent fluxes according to the formulation of Isemer and Hasse.

1. Introduction

Deep convection in the ocean is observed only at a few places worldwide. It drives the thermohaline circulation, which accounts for about 50% of the poleward transport of heat in atmosphere and ocean, and depicts the importance of deep convection for the climate system.

The development of deep convection is forced by air–sea interaction, by losses of heat and water vapor by the surface waters, which leads to a destabilization and consecutively to convection in the ocean. To improve our understanding of the processes leading to and resulting from deep convection the Labrador Sea Experiment (Lab Sea Group 1998) took place. Part of that experiment was the cruise of the R/V Knorr in February/March 1997. A series of oceanographical and meteorological measurements was carried out to investigate air–sea interaction and its role in the development of deep convection.

The objective of the present paper is the analysis of turbulence measurements to obtain the turbulent fluxes of momentum and sensible heat. These estimated fluxes can be used to validate the results of numerical models (Renfrew et al. 2002) or to check whether existing bulk parameterizations (e.g., Bunker 1976; Smith 1980; Large and Pond 1981, 1982; Anderson and Smith 1981; Isemer and Hasse 1987; Smith 1988; Smith et al. 1992; Anderson 1993; DeCosmo et al. 1996) are valid for conditions as observed over the Labrador Sea during wintertime. Therefore, the main goal of the present paper is to analyze measurements of the turbulent fluxes of momentum and sensible heat and to check the validity of existing parameterizations under such conditions.

2. The Labrador Sea Experiment

The primary cruise of the Labrador Sea Experiment took place in February and March 1997 (Fig. 1) on board the R/V Knorr. A mast designed and built especially for purposes of measurements of air–sea interaction was mounted on the foredeck of the R/V Knorr close to the bow (Fig. 2). Turbulence measurements by the Institut für Meereskunde Kiel included a sonic anemometer, mounted on a crossbar at the top of this mast, corresponding to a height of about 18.5 m above the sea surface. This sonic anemometer (manufactured by METEK, Hamburg, Germany) sampled at 30 Hz. The raw data of the three wind components and the temperature were stored. At a lower rate of 5 Hz the roll and pitch angles, measured by a system consisting of oil damped pendulums, were recorded to quantify the ship’s motions due to wind waves and swell. This information was used for a coordinate transformation of the measured longitudinal and lateral wind components.

Mean meteorological sensors were those of the ship’s Improved Meteorological Instrumentation (IMET) measurements system, for example, a pressure sensor, a hy-
grometer, intake temperature, a thermistor, and a cup anemometer. These measurements were taken on the ship’s forecast at a height of about 19.5 m. The ship’s velocity and direction were provided by a gyrocompass and a Doppler log with ship’s position given via GPS.

3. Theory

The turbulent fluxes of momentum were computed using the so-called inertial dissipation method. It is based on the budget of the turbulent kinetic energy $\varepsilon$, which is given here in its nondimensional form (Large and Pond 1982):

$$0 = \Phi_\varepsilon \left( \frac{\varepsilon}{L} \right) - \frac{\varepsilon}{L} \frac{\kappa S}{u^*} \frac{\partial (\varepsilon w)}{\partial z} - \frac{\kappa S}{u^*} \frac{\partial (\varepsilon p)}{\partial z} - \frac{\kappa S}{u^*} \frac{\partial \varepsilon}{\partial z}$$

where $\Phi_\varepsilon$ is a universal stratification function, $\varepsilon$ is the height of measurements, $L$ is the Monin–Obukhov length, $\kappa$ is the von Kármán constant, $w$ the vertical wind component, $p$ the pressure, $\rho$ the air density, $u^*$ the friction velocity, and $\varepsilon$ the dissipation rate. Equation (1) can be solved for $u^*$.

With

$$S(k) = \alpha \varepsilon^{2/3} k^{-5/3}$$

and Taylor’s principle of the frozen turbulence

$$kS(k) = f S(f),$$

where $\alpha$ is the Kolmogoroff constant, $k$ the wavenumber, $f$ the frequency, and $S$ the spectral energy density, we get the friction velocity

$$u^* = \left. \left( \frac{2\pi k}{\langle \epsilon \rangle} \right)^{1/3} \frac{S_{\text{rms}}(f)}{\alpha_{\text{rms}}(2\pi)^{2/3}} \Phi_{\varepsilon} \left( \frac{\varepsilon}{L} \right) \right|_{\frac{\varepsilon}{L}}$$

neglecting the transport term (term 3 of the right-hand side) and the pressure term (term 4 of the right-hand side) according to earlier studies (e.g., Large and Pond).
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**FIG. 2.** Photo of the foreship of R/V *Knorr* taken from the observation deck. Instruments for turbulence measurements are mounted on the t-bar of the bowmast at a height of approximately 18.5 m above sea level. The foremost, which is approximately 11 m behind the bow mast, carries temperature and wind speed sensors of the ship’s IMET.

Here \( \langle u \rangle \) is the mean wind speed. Recent studies have shown the importance of both terms for situations with unstable stratification (e.g., Yelland and Taylor 1996). Therefore, an imbalance term has been introduced (e.g., Yelland and Taylor 1996; Dupuis et al. 1997) for situations with nonneutral stability, which is defined as

\[
\Phi_{\text{imb}} = \kappa \frac{\partial(w_e)}{\partial z} + \kappa \frac{\partial(w_p)}{\partial z}. \tag{5}
\]

When estimating the friction velocity from the budget of the turbulent kinetic energy another problem occurs, because the Monin–Obukhov length also depends on \( u_w \). To solve this problem there are two possibilities: using a bulk parameterization to compute the friction velocity and buoyancy flux and hence obtain the Monin–Obukhov length (e.g., Large and Pond 1982) or to derive \( u_w \) iteratively by making use of the fluxes from the sonic anemometer measurements. Thus, the friction velocity was derived by reinjecting \( u_w \) in the calculation of the Monin–Obukhov length until convergence for \( u_w \) was reached. The latter was suggested by Dupuis et al. (1997). In the following it is called the dissipation–dissipation (DD) algorithm, while the bulk method is called the dissipation–bulk (DB) algorithm.

The inertial dissipation method for buoyancy fluxes is based on the budget of scalar variance (Large and Pond 1982), which under horizontal homogeneous and stationary conditions simplifies to

\[
\langle w T \rangle \frac{\partial T}{\partial z} + \frac{1}{2} \frac{\partial \langle w T^2 \rangle}{\partial z} + N_T = 0. \tag{6}
\]

Neglecting the transport term and applying Eq. (6) to the virtual temperature \( T_v \) instead of the air temperature \( T \) it simplifies to

\[
\langle w T_v \rangle = \left[ \frac{\kappa \bar{u}_w N_{T_v}}{\Phi_{T_v}(z/L)} \right]^{1/2}, \tag{7}
\]

where \( N_T \) and \( N_{T_v} \) are the turbulent dissipation rates for the temperature and virtual temperature variance, and \( \Phi_{T_v} \) is a universal stratification function. Here \( N_T \) or \( N_{T_v} \) can be inferred from spectral energy densities in the inertial subrange according to

\[
S_{T}(f) = \beta_T \varepsilon^{-1/3} N_T \left( \frac{2\pi}{\langle \bar{u} \rangle} \right)^{-2/3} f^{-5/3}, \tag{8}
\]

where \( \beta_T \) is 0.8 (Large and Pond 1982). The von Kármán constant is set to 0.4, and the Kolmogoroff constant \( \alpha \) is set to 0.52 (Högström 1996). The universal stratification functions are adopted from Businger et al. (1971) and Dyer (1974).

Synoptic conditions were characterized by relatively high sea surface temperatures (about 0°–3°C) compared to the low air temperatures (about −15°–0°C). Therefore,
free convection has to be taken into account, which is done according to Gravech et al.
(1998). For that purpose the integrated Businger and Dyer or Kansas-type relationship for unstable conditions was replaced by

\[
\Psi_{\text{Kansas}} + \frac{(z/L)^2 \Psi_{\text{convective}}}{1 + (z/L)^2},
\]

(9)

where

\[
\Psi_{\text{convective}} = \frac{3}{2} \ln(y^2 + y + 1) - \sqrt{3} \arctan\left( \frac{2y + 1}{\sqrt{3}} \right) + \frac{\pi}{\sqrt{3}}.
\]

(10)

Here \( y = [1 - 12.87(z/L)]^{1/3} \) is the stratification function for conditions of free convection. Further, the vector-averaged wind speed was replaced by the scalar-averaged wind speed.

To derive turbulent fluxes making use of the inertial dissipation method a number of conditions have to be fulfilled. First, the dissipation rate must be estimated from spectral energy densities at frequencies in the inertial subrange. The inertial subrange is characterized by spectral energy densities, which are proportional to \( f^{-5/3} \). Second, conditions should be locally isotropic, which is reflected in a ratio of the spectral energy density of the lateral to the longitudinal component of 4:3. All measured spectra were checked for both conditions at frequencies ranging from 3 to 12 Hz to estimate individually for each time series the low and high frequency end of a 3-Hz broad frequency interval, which has the smallest deviations to the \(-5/3\) law and the 4:3 ratio. Time series with deviations of more than 10% from the \(-5/3\) law or ratios of the spectral energy densities of the vertical to the longitudinal wind component less than 1 were ejected. The remaining deviations from local isotropy were corrected following Wucknitz (1978):

The influence of the flow distortion on the measurements by the ship itself, resulting in inaccuracies of wind measurements, was minimized by applying the results of a flow distortion study. This study was performed by the Southampton Oceanography Centre (Moat and Yelland 1998). In summary, the main results of this study were that the vertical displacement of the flow at the sonic site was 0.78 m and the percentage error in wind speed only \(-0.67\%\). The vertical displacement of wind speed measurements of the ship’s IMET was 1.37 m with a percentage error in wind speed of 0.99%. It should be mentioned that the flow distortion study did not investigate the disturbances resulting from the ship’s superstructure, which may also influence turbulence measurements.

Finally, the spectra were checked for spikes. To avoid flow distortion from instruments mounted on the same crossbar, only data where the relative wind direction was within a range of \( \pm 40^\circ \) of the bow, were used.

Sensible heat fluxes were also estimated using the cross-correlation method. The cross-correlation technique is based on measurements of the exchanges in the atmospheric surface layer, where the fluctuating vertical velocity transports air properties up and down. The sensible heat flux \( H \) is defined by

\[
H = \rho c_p \langle w T \rangle,
\]

(11)

where \( c_p \) is the specific heat at constant pressure. Following Reynolds averaging convention, the vertical velocity \( w \) and air temperature \( T \) are separated into a mean (angle brackets) and fluctuation (primes), and are given by \( \langle w \rangle + w' \) and \( T + T' \).

Integration of the \( w, T \) cospectrum over all contributing frequencies gives the covariance or sensible heat flux. Unfortunately, the method is highly sensitive to instrument orientation, which hampers the ability of this method on moving platforms such as ships. An analysis of pitch and roll angles showed that the variation of the pitch angles is on average a factor of 3 smaller than the variation of the roll angles. Therefore, the ship’s motions were estimated approximately only from measurements of the roll angles directly at the sonic anemometer, which were used to compute the local orbital velocity at the instruments location. That simple approach includes the assumption that there is a lack of correlation between the heave and the temperature. Figure 3 shows resulting spectra of the corrected \( u \) and \( w \) components of the wind for a situation with swell (Fig. 4) at a wind speed of approximately 12 m s\(^{-1}\). Since the motions of the ship were not fully corrected, the computed fluxes of sensible heat based on the cross-correlation method are expected to show additional scatter.

Finally, both cross-correlation and dissipation techniques need a correction because temperatures taken
from the sonic anemometer are close to the virtual temperature (Kaimal and Gaynor 1991). This correction was adopted from Dupuis et al. (1997).

4. Results

a. Imbalance term

The imbalance term was deduced from the assumption that at the same wind speed, neutral drag coefficients should not depend on stability. Thus, the whole dataset was divided into a near-neutral ($|z/L| < 0.5$) and an unstable part. A linear regression based on the near-neutral measurements of the drag coefficients on the mean wind speed results in

$$C_{d,\text{in}} = (0.6516 + 0.0524u_{\text{w,ic}}) \times 10^{-3},$$  \hspace{1cm} (12)

by assuming that the imbalance is equal to zero under near-neutral conditions (e.g., Large and Pond 1981; Yeland and Taylor 1996; Dupuis et al. 1997). It should be noted that this assumption does not agree with results reported by Thiermann and Graßl (1992), Frenzen and Vogel (1992), and Edson and Fairall (1998), who found that production generally exceeds dissipation in near-neutral conditions. However, since a number of studies have also found that dissipation exceeds production in near-neutral conditions (e.g., Högström 1990; Smedman et al. 1999), we believe that this is a reasonable assumption with this dataset. The imbalance term can then be derived from the two different estimates of the turbulent fluxes of momentum: the bulk fluxes according to Eq. (12) and the inertial dissipation fluxes. Based on the DD algorithm, taking free convection into account, the imbalance term is calculated by a linear regression to

$$\Phi_{\text{imb}} = -0.73 \frac{z}{L} - 0.16 \hspace{1cm} (13)$$

(Fig. 5) using the whole dataset. The correlation coefficient of $-0.42$ is only low, but according to a Student’s t-test significant at the 99% level. That low correlation might be caused by the fact that most of the time $z/L$ was close to zero due to high observed wind speeds.

This imbalance term agrees well with earlier results of Dupuis et al. (1997), who obtained

$$\Phi_{\text{imb}} = -0.69 \frac{z}{L} - 0.17 \hspace{1cm} (14)$$

taking varying bulk transfer coefficients of heat and free convection into account. This means that the imbalance term increases with increasing deviations from neutral stability, which is in contrast to a study of Edson and Fairall (1998). They estimated the imbalance term from the assumption that for conditions of free convection the imbalance term vanishes. Such different imbalance terms have a strong influence on the resulting drag coefficients. The imbalance term according to Edson and Fairall (1998) gives higher drag coefficients than the imbalance term presented in this study. The differences in the mean are of the order of approximately 10% for conditions as they were observed during this cruise.

b. Drag coefficient

Drag coefficients were determined via the inertial dissipation method from spectra of the longitudinal and vertical wind components. Spectral energy densities were calculated from time series of 17-min length.

Figure 6 shows the results using the DB algorithm, where the parameterization scheme of Liu and Blanc...
(1984) was used to derive Monin–Obukhov length. It is based on the model of Liu et al. (1979). It takes into consideration the interfacial sublayers on both sides of the air–sea interface where molecular constraints are important. The flux-profile relations are matched to the logarithmic profiles. Drag coefficients to estimate the roughness lengths $z_0$ were adopted from Smith (1980); heat fluxes were calculated via roughness Reynolds numbers. The imbalance term was assumed to be negligible for estimating the drag coefficient according to the DB algorithm. A linear regression of the drag coefficients $C_D$ on the mean wind speed gives

$$C_D = (0.4 + 0.085U_{10}) \times 10^{-3},$$  

reduced for neutral stability and 10-m height. The correlation coefficient is 0.82. The standard deviation in the estimates of the regression coefficient is $0.017 \times 10^{-3}$, the intercept is $0.03 \times 10^{-3}$, and the unexplained variance is $0.22 \times 10^{-3}$ in terms of standard deviation.

The regression of the drag coefficients on the mean wind speed fits well with the results given by Smith (1980), although the estimated regression coefficient is higher. Figure 7 shows the same data using the DD algorithm. Introducing an imbalance term according to Eq. (13) and calculating Monin–Obukhov length iteratively and by making use of fluxes estimated from the sonic anemometer measurements, a linear regression of derived drag coefficients on the mean wind speed gives

$$C_D = (0.54 + 0.070U_{10}) \times 10^{-3}$$  

with a correlation coefficient of about 0.72 (Fig. 7). Standard deviation in the estimate of the regression coefficient is $0.018 \times 10^{-3}$, the error of the intercept $0.03 \times 10^{-3}$, and the unexplained variance is $0.21 \times 10^{-3}$ in terms of standard deviation. Results of the DD algorithm are close to results of the DB algorithm. The introduction of the imbalance term influences mostly the drag coefficients at low wind speeds, where the largest deviations from neutral stability occur. This affects mainly the wind speed dependency of the drag coefficients, where Eqs. (15) and (16) represent the extreme values of the regression coefficients from all possible combinations: DB or DD method with or without neglecting the imbalance term. The coefficients given by Smith (1980) fit our result very well.

As expected, the drag coefficients of the present study are significantly lower than those estimated from the Humidity Exchange over the Sea (HEXOS) Main Experiment (HEXMAX; Smith et al. 1992), where due to limited water depths shallow water waves were observed. Such shallow water waves lead to an increased roughness of the sea surface and therefore to enhanced drag coefficients compared to deep water conditions. The presence of swell may also lead to an increase in the drag coefficient, as recent studies from Janssen (1999) have shown. Swell was observed during the cruise in two manners: visual and with the aid of measurements of the ship’s vertical displacement (Fig. 4), where an additional peak at low frequencies was taken as an indicator of the presence of swell. Although the small number of available measurements for situations with swell does not allow comprehensive investigations of the influence of the swell, Fig. 7 indicates no significant change in the drag coefficient for cases with swell compared with measurements in the absence of swell. This is supported by a study of Rutgersson et al. (2000), who showed that swell should have a significant influence on the air–sea fluxes only under stable con-
plained variance is 60 W m$^{-2}$, the correlation coefficient is about 0.84. The unexplained variance slightly on the magnitude of the sensible heat flux itself; of both variables, shows only small deviations from the measurement system. To the problem of excluding exactly the motions reducable comparison of the methods might be due to uncertainties in heat flux. We suggest that the differences in the comparison of the two methods is low. Standard deviation between simultaneous cross-correlation and dissipation estimates for the inertial dissipation method. Compared to those values the bias of 9 W m$^{-2}$ between the results of both different methods is low. Standard deviation between simultaneous cross-correlation and dissipation estimates is 55 W m$^{-2}$, which is about 26% of the average sensible heat flux. We suggest that the differences in the comparison of the methods might be due to uncertainties in the cross-correlation fluxes. That is primarily reducable to the problem of excluding exactly the motions resulting from wind waves and swell due to the limitations of the measurement system.

A neutral linear regression, minimizing the variances of both variables, shows only small deviations from the 1:1 line (Fig. 8, Table 1). Differences depend only slightly on the magnitude of the sensible heat flux itself; the correlation coefficient is about 0.84. The unexplained variance is 60 W m$^{-2}$ in terms of standard de-

c. Sensible heat flux

Sensible heat fluxes were computed using both the cross-correlation and the inertial dissipation methods. Figure 8 compares the results of the two methods. It is obvious that sensible heat fluxes are generally high due to the prevalent weather conditions over the Labrador Sea in wintertime, that is, a large number of days with large air–sea temperature differences and high wind speeds. That is reflected in sensible heat fluxes reaching about 500 W m$^{-2}$ and more.

The average estimated sensible heat flux is 200 W m$^{-2}$ for the cross-correlation method and 209 W m$^{-2}$ for the inertial dissipation method. Compared to those values the bias of 9 W m$^{-2}$ between the results of both different methods is low. Standard deviation between simultaneous cross-correlation and dissipation estimates is 55 W m$^{-2}$, which is about 26% of the average sensible heat flux. We suggest that the differences in the comparison of the methods might be due to uncertainties in the cross-correlation fluxes. That is primarily reducable to the problem of excluding exactly the motions resulting from wind waves and swell due to the limitations of the measurement system.

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Fig. 9. Sensible heat fluxes estimated using the cross-correlation method compared to sensible heat fluxes calculated by applying a bulk parameterization on the mean values of air temperature, wind speed, and SST. The solid line shows the results of a linear regression; the dotted line indicates the 1:1 line. Bulk transfer coefficients (a) from Isemer and Hasse (1987) and (b) from Large and Pond (1981, 1982).

The measured sensible heat fluxes have also been compared with parameterized fluxes using bulk transfer coefficients from Smith (1988), Bunker (1976), DeCosmo et al. (1996) using drag coefficients according to Smith (1980), Anderson and Smith (1981), and Anderson (1993). Summarized results are given in Table 1. Compared with dissipation sensible heat fluxes, the Bunker parameterization overestimates fluxes by 13%. Parameterizations according to Anderson and Smith (1981), DeCosmo et al. (1996), and Anderson (1993) underestimate the measured fluxes by approximately 10%; those of Large and Pond (1982) and Smith (1988) underestimate sensible heat fluxes by more than 18% and 34% compared to estimates based on the inertial dissipation method.

The better agreement between dissipation sensible heat fluxes and parameterized heat fluxes than between cross-correlation sensible heat fluxes and parameterized heat fluxes in terms of correlation coefficient suggests that cross-correlation heat fluxes are less accurate than dissipation sensible heat fluxes. Sensible heat fluxes are also available from numerical weather prediction. In general these fluxes are considerably higher than fluxes estimated from our measurements. Close to the ice edge they reach values of about 800 W m⁻² (Renfrew et al. 2002). This might be caused partly by the algorithms used in numerical models to estimate air–sea interaction.

5. Summary

Estimated drag coefficients using the inertial dissipation method agree well with results of earlier studies as given, for example, by Smith (1980). For conditions found over the Labrador Sea in wintertime the dissim...
Sensible heat fluxes were estimated using two different methods, the cross-correlation technique and the inertial dissipation method. The results from both methods agree well, indicating that the inertial dissipation method is very useful for analyzing measurements on moving platforms. It was found that the often used bulk transfer coefficients for sensible heat of Large and Pond (1982) or of Smith (1988) lead to a considerable underestimation of sensible heat fluxes under the conditions experienced over the Labrador Sea in winter, that is, large air–sea temperature differences and high wind speeds. Parameterizations according to Isemer and Hasse (1987), Anderson and Smith (1981), DeCosmo et al. (1996), and Anderson (1993) give reasonable results for an area like the Labrador Sea during wintertime.

The datasets above are a useful tool to validate the model output of numerical models or reanalysis data in areas like the Labrador Sea, where direct measurements of air–sea interaction are sparse.

That has been done in a study of Renfrew et al. (2002), which gives detailed comparisons of standard meteorological observations and estimated fluxes with model outputs of the National Centers for Environmental Prediction–National Center for Atmospheric Research (NCEP–NCAR) and European Centre for Medium-Range Weather Forecasts (ECMWF) reanalysis projects.

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